

Chapter 1

1.1 Assume that there are two algorithms A and B for a given problem P . The time complexity functions of algorithms A and B are $5n$ and $\log_2 n$ respectively. Which algorithm should be selected assuming that all other conditions remain the same for both the algorithms?

Solution:

\Rightarrow For all values of ' n ', $\log_2 n$ is smaller than $5n$.

For example, for $n=1024$, $\log_2 1024 = 10$ but $5n = 5(1024) = 5120$ operations.

Therefore, Algorithm B having complexity $\log_2 n$ is preferred.

1.2 Let us assume that for a telephone directory problem P , three algorithms exist, A , B and C . Time complexities of A , B and C are $3n$, $5n$ and $\log n$ respectively. Assume that the input instance n is $10^5 \cdot 10^3$. Assume that the machine executes 10^9 instructions per second. How much time will algorithms A , B and C take? Which algorithm will be the best?

Solution:

\Rightarrow Here $n = 10^5 \cdot 10^3$. At computer executes 10^9 instruction / sec.

$$\therefore \text{Time}_A = \frac{3(10^3)}{10^9} = \frac{3}{10^6} = 0.000003 \text{ Sec}$$

$$\text{Time}_B = \frac{5(10^3)}{10^9} = \frac{5}{10^6} = 0.000005 \text{ Sec}$$

$$\text{Time}_C = \frac{\log(10^3)}{10^9}$$

$$\text{Assuming base 10, } \frac{\log_{10} 10^3}{10^9} = \frac{3}{10^9} = 0.000000003 \text{ Sec}$$

\therefore Third algorithm is best one.